# A novel approach to competing risks analysis using case-base sampling

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# Acknowledgements

This project is joint work with:

- Sahir Bhatnagar
- Olli Saarela (U. Toronto)
- Jim Hanley

# Introduction

 In epidemiological studies of time-to-event data, a quantity of interest to the clinician and the patient is the absolute risk of an event, e.g. 5-year risk of developing cancer.

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- In some settings, the analysis is complicated by the presence of competing events (e.g. complications due to bone-marrow transplant in a study of acute leukemia recurrence).
- A proper estimation of absolute risks needs to take these competing events into account.

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- A common alternative is the Cox proportional hazards model.
  - However, this model leads to a two-step procedure for estimating the hazard function.

• We propose a **simple** approach to modeling **directly** the cause-specific hazards using (smooth) parametric families.

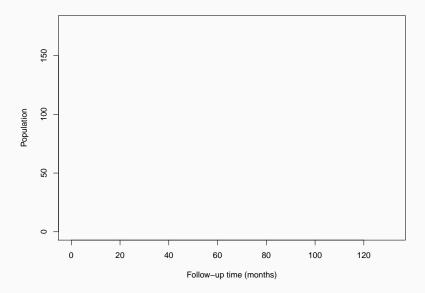
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  - Our approach relies on Hanley & Miettinen's case base sampling method [1].

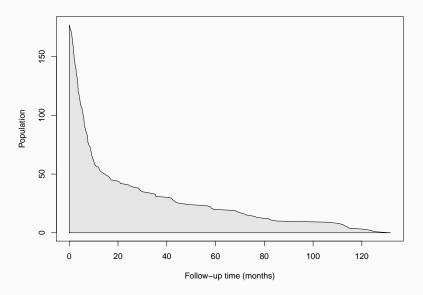
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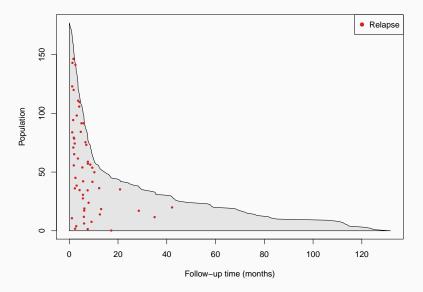
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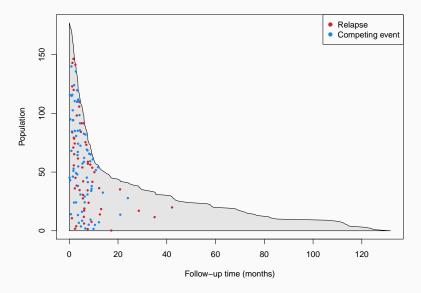
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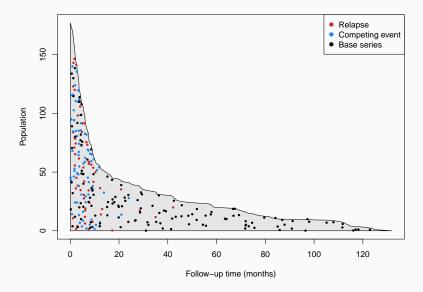
This method is currently available as an R package: http://sahirbhatnagar.com/casebase/











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- Case-base sampling reduces the model fitting to a familiar multinomial regression.
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- By sampling a large base series, the information loss eventually becomes negligible.
- This framework can easily be used with time-varying covariates (e.g. time-varying exposure).

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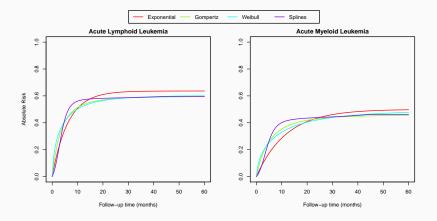
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- Weibull:  $g(t; \alpha) = \alpha \log t$ .

Data analysis

## Data

Variable description	Statistical summary	
Sex	M=Male (100)	
	F=Female (77)	
Disease	ALL (73)	
	AML (104)	
Phase	CR1 (47)	
	CR2 (45)	
	CR3 (12)	
	Relapse (73)	
Type of transplant	BM+PB (21)	
	PB (156)	
Age of patient (years)	4–62	
	30.47 (13.04)	
Failure time (months)	0.13-131.77	
	20.28 (30.78)	
Status indicator	0=censored (46)	
	1=relapse (56)	
	2=competing event (75)	



Absolute risk for female patient, median age, in relapse at transplant (stem cells from peripheral blood).

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Variable	Hazard ratio	95% CI
Sex	0.68	(0.39, 1.20)
Disease	0.51	(0.28, 0.92)
Phase CR2	1.18	(0.47, 2.96)
Phase CR3	1.51	(0.39, 5.86)
Phase Relapse	4.38	(2.01, 9.54)
Source	1.37	(0.45, 4.23)
Age	0.99	(0.97, 1.02)

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- We are explicitly modeling time, and we cant therefore how to model the effect of time on the hazard function.
- We can test the significance of covariates, in a similar way to traditional competing risks approaches.

### References I



J. A. Hanley and O. S. Miettinen.

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The International Journal of Biostatistics, 5(1), 2009.



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#### References II



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Bone marrow transplantation, 45(9):1388–1395, 2010.

Questions or comments?

For more details, visit

http://sahirbhatnagar.com/casebase/